Concavity and Inflection Points (Calculator Active)

1997 #77

The graph of the function $y = x^3 + 6x^2 + 7x - 2\cos x$ changes concavity at x =

2008 #80

The derivative of the function *f* is given by $f'(x) = x^2 \cos(x^2)$. How many points of inflection does the graph of *f* have on the open interval (-2, 2)?

| (A) One | (B) Two | (C) Three | (D) Four | (E) Five |
|---------|---------|-----------|----------|----------|
|---------|---------|-----------|----------|----------|

2008 #90

The function *f* is continuous on the closed interval [2, 4] and twice differentiable on the open interval (2, 4). If f'(3) = 2 and f''(x) < 0 on the open interval (2, 4), which of the following could be a table of values for *f*?

| (A) (| (B) | (C) | (D) | (E) |
|---|--|--|---|---|
| $ \begin{array}{c ccc} x & f(x) \\ 2 & 2.5 \\ 3 & 5 \\ 4 & 6.5 \\ \end{array} $ | $ \begin{array}{c cc} x & f(x) \\ \hline 2 & 2.5 \\ \hline 3 & 5 \\ \hline 4 & 7 \end{array} $ | $ \begin{array}{c ccc} x & f(x) \\ 2 & 3 \\ 3 & 5 \\ 4 & 6.5 \end{array} $ | $ \begin{array}{c ccc} x & f(x) \\ \hline 2 & 3 \\ \hline 3 & 5 \\ \hline 4 & 7 \end{array} $ | $ \begin{array}{c ccc} x & f(x) \\ 2 & 3.5 \\ 3 & 5 \\ 4 & 7.5 \\ \end{array} $ |

2003 #90

For all x in the closed interval [2, 5], the function f has a positive first derivative and a negative second derivative. Which of the following could be a table of values for f?

| (A) | (B) | (C) | (D) | (E) |
|---|---|--|---|--|
| $ \begin{array}{c ccc} x & f(x) \\ \hline 2 & 7 \\ \hline 3 & 9 \\ \hline 4 & 12 \\ \end{array} $ | $ \begin{array}{c ccc} x & f(x) \\ \hline 2 & 7 \\ \hline 3 & 11 \\ \hline 4 & 14 \end{array} $ | $ \begin{array}{c cc} x & f(x) \\ \hline 2 & 16 \\ \hline 3 & 12 \\ \hline 4 & 9 \end{array} $ | $ \begin{array}{c ccc} x & f(x) \\ \hline 2 & 16 \\ \hline 3 & 14 \\ \hline 4 & 11 \\ \end{array} $ | $ \begin{array}{c ccc} x & f(x) \\ \hline 2 & 16 \\ \hline 3 & 13 \\ \hline 4 & 10 \end{array} $ |
| 5 16 | 5 16 | 5 7 | 5 7 | 5 7 |