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4.3 MODELING & OPTIMIZATION

§4.3 Optimization Problems:

Solve these on your own paper in your notebook.

#2:

Find two positive numbers that minimize the sum of twice the first number and the second, if the product of the two numbers is 288.

#3:

What are the dimensions of a closed cylindrical can that can hold 40 cubic inches of liquid and uses the least amount of material?

#4:

A rancher has 200 feet of fencing to enclose two rectangular fields as shown in the diagram. What are the dimensions of the field that maximize the area?

x x

#5

Find two positive integers whose sum is 20 and whose product is as large as possible.

#6:

An oil can is to be made in the form of a right circular cylinder to contain 1 quart of oil. What dimensions of the can will require the least amount of material? (1 quart liquid = 57.75 cubic inches)

#7:

If you have 100 feet of fencing and you want to enclose a rectangular area adjacent to the long side of the barn, what is the largest area you can enclose?

#8:

The product of two positive numbers is 192. Find the two numbers such that the sum of the first and three times the second is a minimum.

#9:

A right circular cylinder is to be designed to hold 12 fluid ounces using the least amount of material. Find the dimensions of the cylinder. (1 fluid ounce = 1.80469 cubic inches)

#10:

A glass fish tank is to be constructed to hold 72 cubic feet of water. It's base and sides are to be rectangular. The top of the tank is open, of course. The width is 5 ft but the length and depth are variable. Building the tank costs \$10/sqft for the base and \$5/sqft for the lateral sides. Find cost and the dimensions of the tank that minimize the cost.

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#11:

Find the point on the parabola $x = -y^2$ that is closest to the point (0,-3).

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#12:

Find the area and the dimensions of a rectangle bounded by the function $y = \cos(x)$ and the x-axis whose area is maximized.

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#13:

Find the area and dimensions of a rectangle bounded by the curve $y = -x^2 + 4$ and the x-axis and y-axis whose area is maximized.



