

Ch 6 Building Area Functions - part I & part II

- Graph $f(t)$ on the coordinate grid & identify $f(a)$ at the lower limit $x = a$.
- Shade the region indicated by the integral and use geometry to find a formula for the area bounded by the function, the x-axis and the limits of integration.
- Simplify the function to a standard form polynomial: $y = a_0x^n + a_1x^{n-1} + \dots + a_{n-2}x^2 + a_{n-1}x^1 + a_n$
- Use a colored pencil to shade the area corresponding to $x=0$.
- Complete the table of values for the area function, $A(x)$. Does the table model the geometric area shown on the graph?

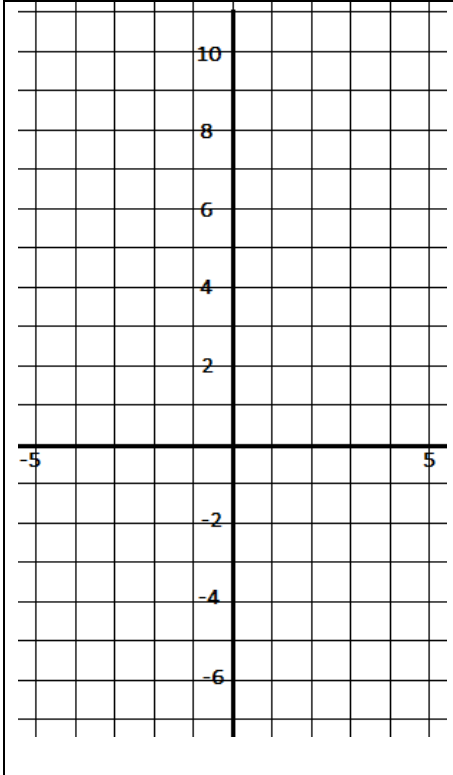
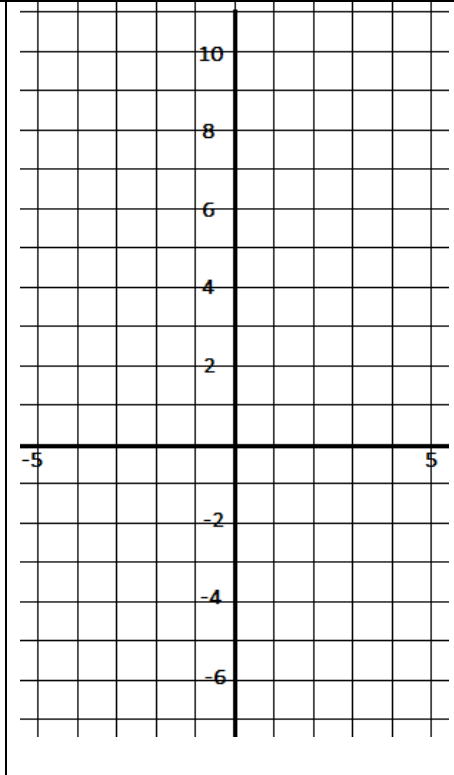
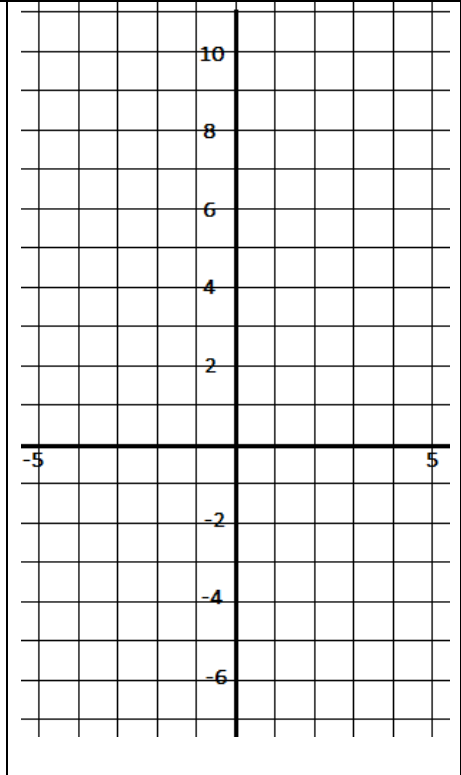
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Looking for Patterns & Making Conjectures:

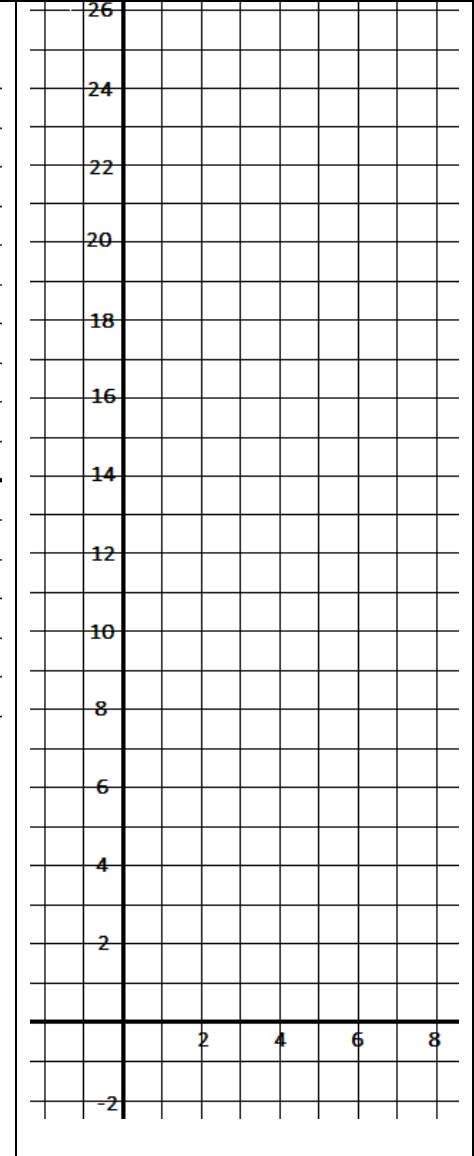
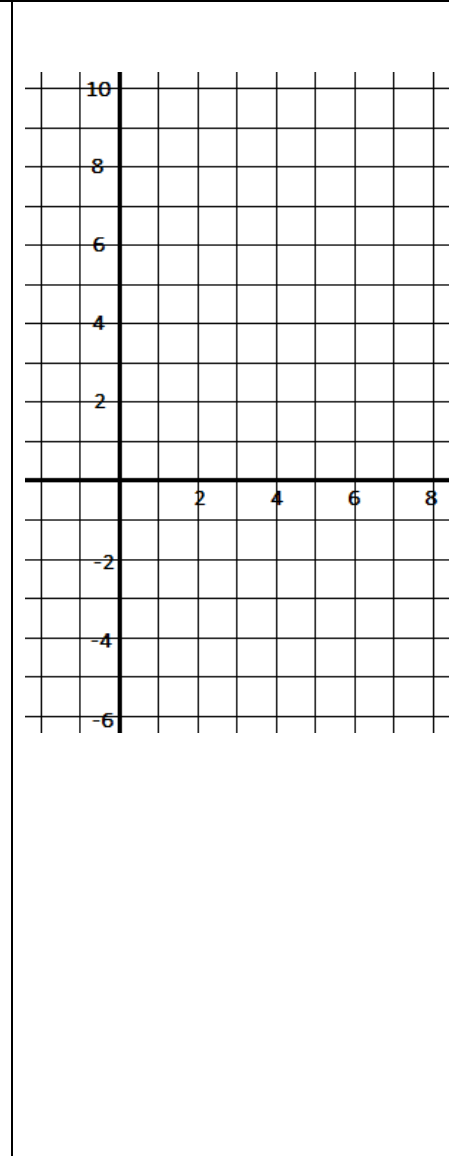
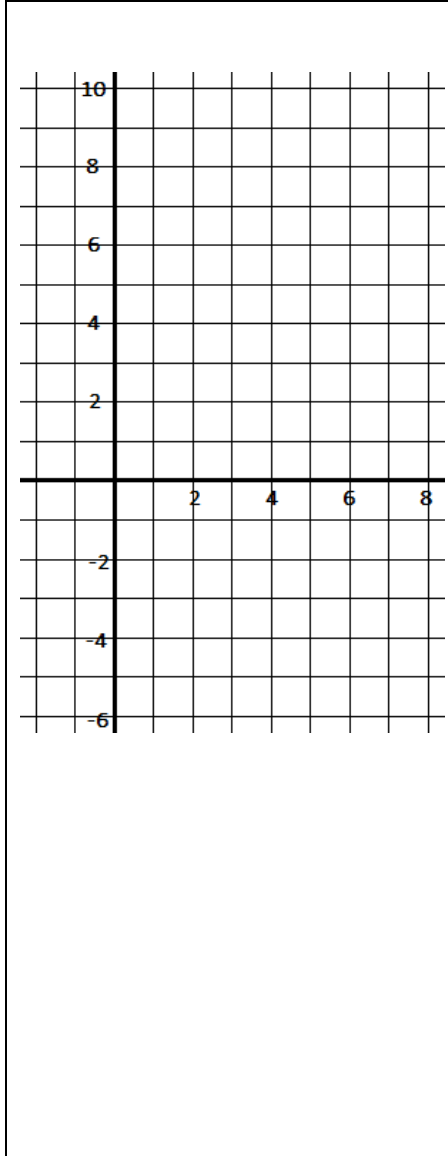
- How is the y-intercept of the $A(x)$ equation and the table related to an area on the graph?
- What is the relationship between the Area function, $A(x)$ and the original function, $f(t)$?
- How are the area functions in (a), (b) & (c) of this set related to each other?

Complete the next three sets of the graphs and tables. After completing each set return to answer these “Making Conjectures:” questions.

<p>2a) $f(t) = t$ on $[0, x]$ $A(x) = \int_0^x t dt$</p>	<p>2b) $f(t) = t$ on $[2, x]$ $A(x) = \int_2^x t dt$</p>	<p>2c) $f(t) = t$ on $[-3, x]$ $A(x) = \int_{-3}^x t dt$</p>																																																
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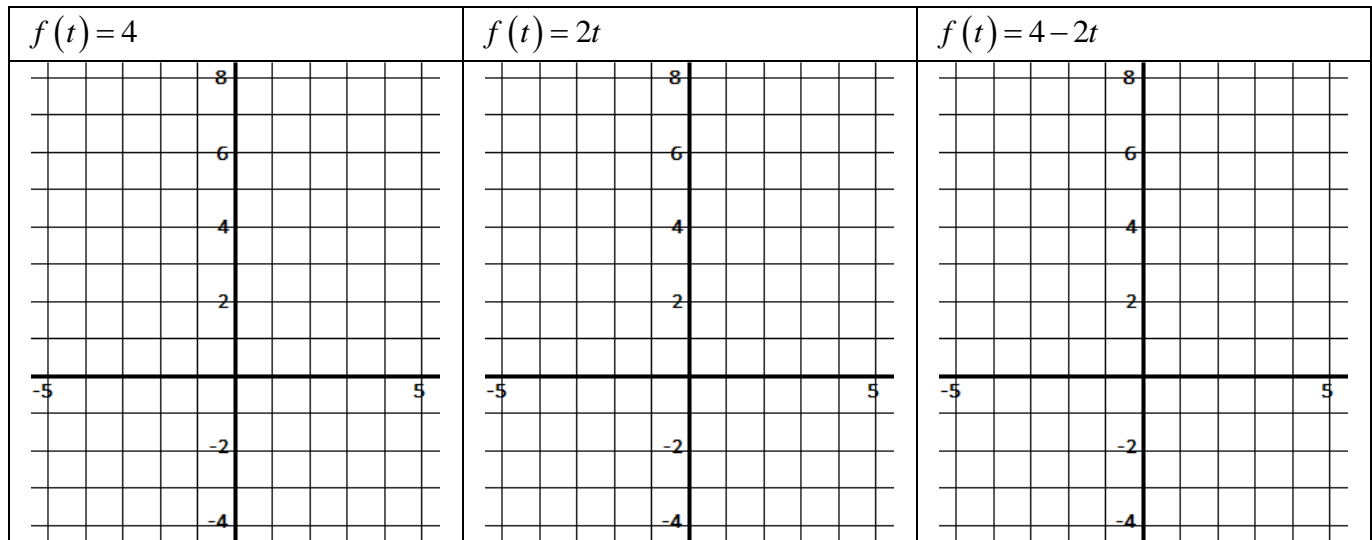
Ch 6 Building Area Functions - part III

We have now seen how to build area functions by:

- Graphing and using geometry to write an area function
- Using a table to record geometric area on the graph and making sure the area function models the data in the table.
- Find the ANTI-DERIVATIVE of $f(t)$, call this $F(x)$ and then evaluate from $x = a$ to $x = b$ according to the following:

$$A(x) = \int_a^b f(t) = F(t) \Big|_a^b = F(b) - F(a)$$

Graph the three functions, $f(t)$, on the grids provided.



Use the graphs above to determine an area function for each integral below. Note the changes in the lower limits of each integral.

$A(x) = \int_0^x (4) dt$	$A(x) = \int_0^x (2t) dt$	$A(x) = \int_0^x (4 - 2t) dt$																																				
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