AP Calculus Final Exam Review #1

(Non-Calculator)

1. Find the derivative of each function:

a.
$$y = x \cos x$$

b. $f(x) = \frac{x^3}{x+1}$
c. $h(x) = 8x - 4 + 2 \ln x$
d. $g(x) = \tan(x^2 + e^{3x})$
f. $y = \ln(3x^4 + 5x)$

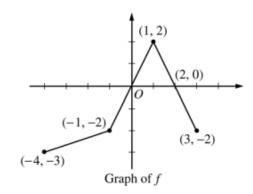
- 2. Write the equation of the line tangent to $h(x) = 8x 4 + 2 \ln x$ at x = 1.
- 3. Let f be the function given by $f(x) = 27x x^3$. On what intervals does f increase?
- 4. Find all critical points and local extrema for $f(x) = \frac{x}{x^2 + 1}$.
- 5. Find all critical points and local extrema for $g(x) = xe^{-3x}$.
- 6. Find all critical points and inflection points for $f(x) = x^3 9x^2 + 24x + 5$.
- 7. Let $f(x) = \begin{cases} \frac{x^2 4}{x 2}, & x \neq 2 \\ k, & x = 2 \end{cases}$. What value of k will make f continuous at x = 2?
- 8. A car comes to a stop five seconds after the driver applies the brakes. While the brakes are on, the velocities in the table are recorded.

Time (in sec)	0	1	2	3	4	5
Velocity (ft/sec)	88	60	40	25	10	0

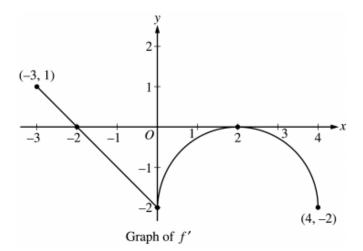
- a. Use a Left Hand Sum to approximate the distance traveled.
- b. Use a Right Hand Sum to approximate the distance traveled.
- c. Which of these is an overestimate? Explain.
- 9. A particle moves along the *x*-axis. The velocity of the particle at time *t* is $8t t^2$. What is the total distance traveled by the particle from time t = 0 to t = 2?
- 10. Find the antiderivative of each function:
 - a. $\int \csc x \cot x \, dx$ b. $\int \sin x \, dx$ c. $\int e^x \, dx$ d. $\int e^{\frac{x}{3}} \, dx$ e. $\int \sec x \tan x \, dx$ f. $\int \frac{1}{2x} \, dx$ g. $\int \frac{12x^3 + 5}{3x^4 + 5x} \, dx$ h. $\int e^{\sin x} \cos x \, dx$
- 11. Evaluate each definite integral:

a.
$$\int_{3}^{9} e^{x/3} dx$$
 b. $\int_{\pi/3}^{\pi} \sin x$ c. $\int_{1}^{e} \frac{1}{2x} dx$

- 12. Pollution is removed from a lake on day t at a rate of f(t) kg/day.
 - a. Explain the meaning of the statement f(12) = 500.
 - b. If $\int_{5}^{15} f(t)dt = 4000$, give the units of the 5, the 15, and the 4000.
 - c. Give the meaning of $\int_{5}^{15} f(t)dt = 4000$.



- The graph of the function f above consists of three line segments.
 - (a) Let g be the function given by $g(x) = \int_{-4}^{x} f(t) dt$. For each of g(-1), g'(-1), and g''(-1), find the value or state that it does not exist.
 - (b) For the function g defined in part (a), find the x-coordinate of each point of inflection of the graph of g on the open interval -4 < x < 3. Explain your reasoning.
 - (c) Let h be the function given by $h(x) = \int_x^3 f(t) dt$. Find all values of x in the closed interval $-4 \le x \le 3$ for which h(x) = 0.
 - (d) For the function h defined in part (c), find all intervals on which h is decreasing. Explain your reasoning.



- 4. Let f be a function defined on the closed interval $-3 \le x \le 4$ with f(0) = 3. The graph of f', the derivative of f, consists of one line segment and a semicircle, as shown above.
 - (a) On what intervals, if any, is f increasing? Justify your answer.
 - (b) Find the *x*-coordinate of each point of inflection of the graph of *f* on the open interval -3 < x < 4. Justify your answer.
 - (c) Find an equation for the line tangent to the graph of f at the point (0, 3).
 - (d) Find f(-3) and f(4). Show the work that leads to your answers.